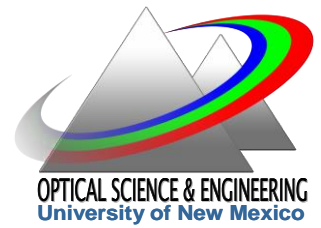


Laser Physics I (PHYC/ECE 464)
FALL 2021



Final Exam

Closed Book, Closed Notes, Calculator will be provided.

Time: 4:00 – 6:00 pm

NAME
last *first*

Score

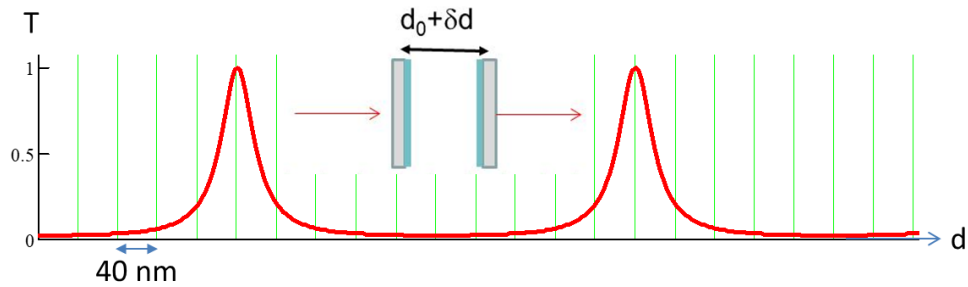
Total= 100 points

Please staple and return these pages with your exam.

Instructor: M. Sheik-Bahae

1. (20 points)

Drawn to scale in the graph below is the power transmission of a scanning symmetric Fabri-Perot (FP) cavity as the distance d is varied from its initial $d_0 \approx 0.5\text{cm}$. The source is a single wavelength laser fixed at wavelength λ_0 . (Assume $n=1$).



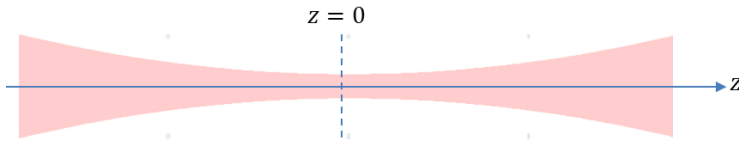
(a) What is λ_0 ?

(b) Estimate the *Finesse* and $\Delta\nu_{1/2}$ (in Hz).

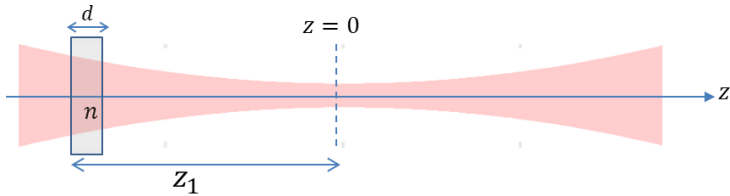
(c) What is the reflectivity (R) of the mirrors?

(d) If reflectivity R were to change to $\sim 85\%$, what will be the new $\Delta\nu_{1/2}$? Draw the approximate transmission curve versus d for this case on top of the graph above.

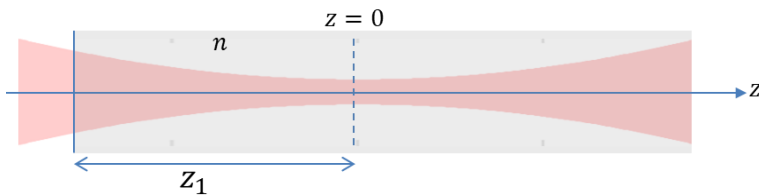
2. (25 points) Consider a fundamental Gaussian beam with known z_0 and wavelength λ_0 travelling from left to right, as shown below.



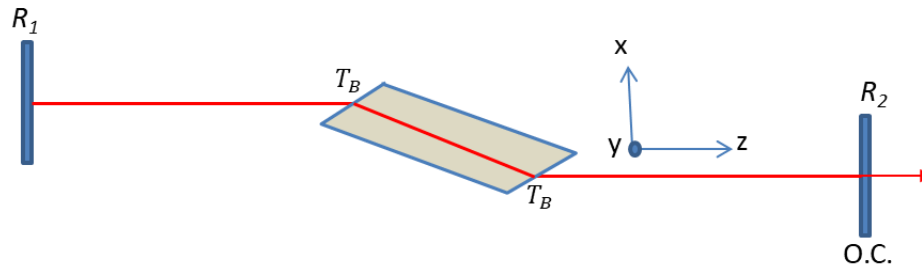
- (a) A glass window of thickness d and index of refraction n is inserted at a distance z_1 prior to $z=0$ (focus) plane as shown. Derive the distance (Δz) and the direction (*sign*) by which the new focal point shifts. What is the new z_0 and the beam waist (w_0) (do they change at all)?



- (b) Repeat part (a) for the case when the original Gaussian beam enters a material of index n with infinite thickness- as shown below. What is the new z_0 and the beam waist (w_0)?



3. (25 points) Consider the solid-state laser system below. The linear cavity parameters are: $R_1=0.99$ and $R_2=0.95$. The gain crystal is cut at Brewster angle to minimize reflective losses but it still has a transmission $T_B=0.998$ per surface.



(a) What is the survival factor S of the passive cavity and the threshold integrated gain ($\gamma_{th}l_g = g_{th}$)?

(b) Express cavity losses $(1-S)$ as $\approx T_2 + L_i$. What is L_i ? Find the needed integrated gain (g_0) for which the existing output coupling is optimum.

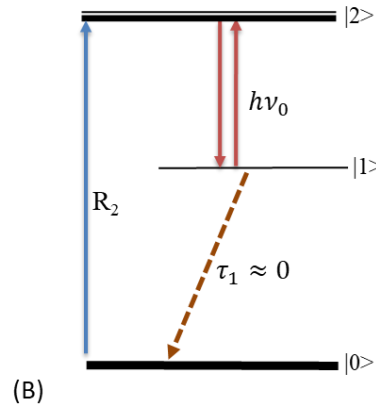
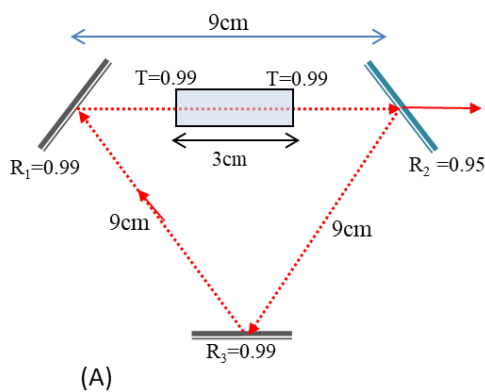
(c) What is the preferred direction of polarization (X, Y or Z) of this laser, and why?

(d) Estimate the narrowest single-mode CW linewidth (in Hz) that can be achieved if this laser outputs $1W$ after stabilization. Assume a cavity roundtrip time (τ_{RT}) of 1 ns .

4. (30 points) Consider the following *unidirectional* ring laser. Cavity parameters are given in the Fig. A. The following parameters are known for the *homogeneously* broadened gain medium:

$$\Delta\nu \approx 2 \times 10^{13} \text{ Hz}; \quad \lambda_0 = 1 \text{ }\mu\text{m}; \quad \sigma_{21}(\nu_0) = 3 \times 10^{-17} \text{ cm}^2; \quad \tau_1 \approx 0; \quad \tau_2 \approx 1 \text{ }\mu\text{s}; \quad g_1 = g_2$$

$$\text{beam area } A = 10^{-4} \text{ cm}^2; \quad n(\text{gain medium}) = 2$$



- (a) What is the threshold upper state population (N_2^{th})?
- (b) What is the **cw output power** if this laser were to be pumped $\times 9$ above the threshold? Assume (and justify) high-Q cavity approximation. Ignore the transmission (leakage) through high reflectivity mirrors.
- (c) Estimate the **excitation pump power (in Watts)** required to sustain the output power in (b). Assume that the lower laser state (level 1 in Fig. B) is 2 eV above the ground state.
- (d) If this laser were to be **cw-modelocked**, describe (and graph) the temporal behavior of the output pulse-train. Assume the shortest possible pulse and ignore dispersion. Estimate the number of longitudinal modes that are oscillating. Estimate the peak output power if pumped at $\times 9$ above the threshold.
- (e) If this laser were to be **Q-switched**, estimate the pulse width. Quantitatively draw a typical such pulse.
- (f) Repeat part (b) if this ring laser were to operate *bi-directional*.